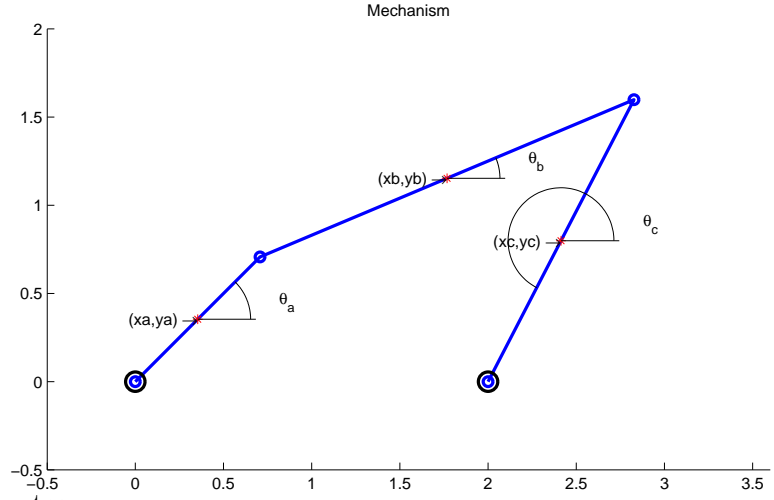


Data:

- $\theta_{a0} = 45^\circ$
- $L_a = 1$
- $L_b = 2.3$
- $L_c = 1.8$
- $L_d = 2$



Generalized coordinates:

$$\mathbf{q}(t) = [x_a \ y_a \ \theta_{a0} \ x_b \ y_b \ \theta_{b0} \ x_c \ y_c \ \theta_{c0} \ x_d \ y_d]^T$$

Constraints:

$$\Phi(\mathbf{q}(t), t) = \left\{ \begin{array}{l} x_a - \frac{L_2 \cos(\theta_a)}{2} \\ y_a - \frac{L_2 \sin(\theta_a)}{2} \\ x_b - x_a - \frac{L_2 \cos(\theta_a)}{2} - \frac{L_3 \cos(\theta_b)}{2} \\ y_b - y_a - \frac{L_2 \sin(\theta_a)}{2} - \frac{L_3 \sin(\theta_b)}{2} \\ x_c - x_b - \frac{L_3 \cos(\theta_b)}{2} - \frac{L_4 \cos(\theta_c)}{2} \\ y_c - y_b - \frac{L_3 \sin(\theta_b)}{2} - \frac{L_4 \sin(\theta_c)}{2} \\ L_1 - x_c - \frac{L_4 \cos(\theta_c)}{2} \\ -y_c - \frac{L_4 \sin(\theta_c)}{2} \\ x_d - x_a - \frac{L_5 \cos(\beta + \theta_b)}{2} - \frac{L_2 \cos(\theta_a)}{2} \\ y_d - y_a - \frac{L_5 \sin(\beta + \theta_b)}{2} - \frac{L_2 \sin(\theta_a)}{2} \\ \theta_a - \theta_{a0} - t w \end{array} \right.$$

Velocities:

$$\Phi_{\mathbf{q}} = \begin{pmatrix} 1 & 0 & \frac{L2 \sin(\theta_a)}{2} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & -\frac{L2 \cos(\theta_a)}{2} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -1 & 0 & \frac{L2 \sin(\theta_a)}{2} & 1 & 0 & \frac{L3 \sin(\theta_b)}{2} & 0 & 0 & 0 & 0 & 0 \\ 0 & -1 & -\frac{L2 \cos(\theta_a)}{2} & 0 & 1 & -\frac{L3 \cos(\theta_b)}{2} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & -1 & 0 & \frac{L3 \sin(\theta_b)}{2} & 1 & 0 & \frac{L4 \sin(\theta_c)}{2} & 0 & 0 \\ 0 & 0 & 0 & 0 & -1 & -\frac{L3 \cos(\theta_b)}{2} & 0 & 1 & -\frac{L4 \cos(\theta_c)}{2} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 & \frac{L4 \sin(\theta_c)}{2} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & -\frac{L4 \cos(\theta_c)}{2} & 0 & 0 \\ -1 & 0 & \frac{L2 \sin(\theta_a)}{2} & 0 & 0 & \frac{L5 \sin(\beta + \theta_b)}{2} & 0 & 0 & 0 & 1 & 0 \\ 0 & -1 & -\frac{L2 \cos(\theta_a)}{2} & 0 & 0 & -\frac{L5 \cos(\beta + \theta_b)}{2} & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\Phi_{\mathbf{t}} = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ -w \end{pmatrix}$$

Accelerations:

$$\gamma = \begin{pmatrix} -\frac{L2 \dot{\theta}_a^2 \cos(\theta_a)}{2} \\ -\frac{L2 \dot{\theta}_a^2 \sin(\theta_a)}{2} \\ -\frac{L2 \cos(\theta_a) \dot{\theta}_a^2}{2} - \frac{L3 \cos(\theta_b) \dot{\theta}_b^2}{2} \\ -\frac{L2 \sin(\theta_a) \dot{\theta}_a^2}{2} - \frac{L3 \sin(\theta_b) \dot{\theta}_b^2}{2} \\ -\frac{L3 \cos(\theta_b) \dot{\theta}_b^2}{2} - \frac{L4 \cos(\theta_c) \dot{\theta}_c^2}{2} \\ -\frac{L3 \sin(\theta_b) \dot{\theta}_b^2}{2} - \frac{L4 \sin(\theta_c) \dot{\theta}_c^2}{2} \\ -\frac{L4 \dot{\theta}_c^2 \cos(\theta_c)}{2} \\ -\frac{L4 \dot{\theta}_c^2 \sin(\theta_c)}{2} \\ -\frac{L2 \cos(\theta_a) \dot{\theta}_a^2}{2} - \frac{L5 \cos(\beta + \theta_b) \dot{\theta}_b^2}{2} \\ -\frac{L2 \sin(\theta_a) \dot{\theta}_a^2}{2} - \frac{L5 \sin(\beta + \theta_b) \dot{\theta}_b^2}{2} \\ 0 \end{pmatrix}$$